

Vector Addition and Subtraction

Unit 3: Vectors and Projectile Motion

Vector Review: Is this a scalar, or a vector?

- A car costs \$52,000.
 - Scalar
- It takes the car 3.9 seconds to reach 100 km/h.
 - Scalar
- The car is driving 90 km/h to the east.
 - Vector
- The car has 38 litres of gasoline.
 - Scalar
- The car drove on 256 kilometres of road from Montreal to Quebec.
 - Scalar
- Quebec is 232 kilometres northeast of Montreal.
 - Scalar

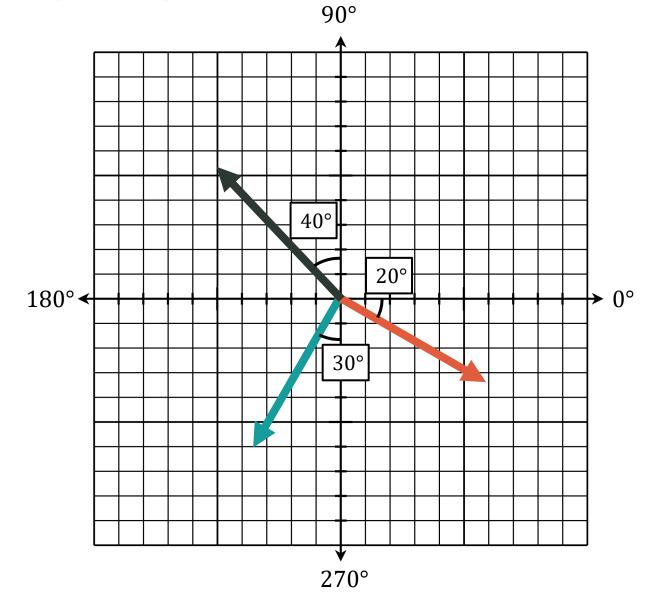
Vector Review: Vector Notation

The following vectors represent the wind's angle as indicated by a weathervane. Express these vectors' direction using the **trigonometric angle**.

1.
$$\theta = 270^{\circ} - 30^{\circ} = 240^{\circ}$$

2.
$$\theta = 360^{\circ} - 20^{\circ} = 340^{\circ}$$

3.
$$\theta = 90^{\circ} + 40^{\circ} = 130^{\circ}$$



Vector Review: Components Calculate the *x* **and** *y* **components of the following force vectors!**

$$\vec{F}_1 = 166 \text{ N} [125^\circ]$$

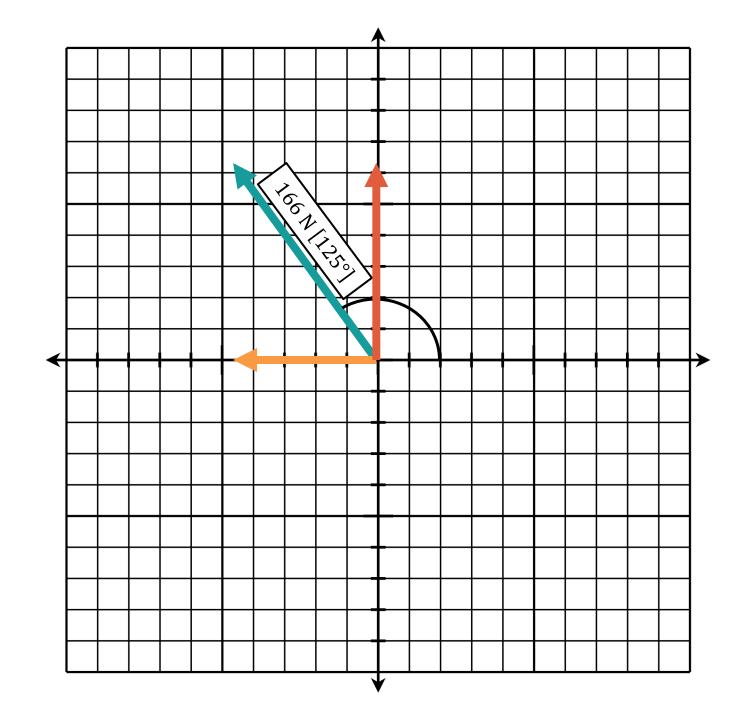
$$F_{x} = (166 \text{ N}) \cos 125^{\circ}$$

= -95.2 N

$$F_y = (166 \text{ N}) \sin 125^\circ$$

= 136 N

$$\vec{F}_1 = (-95.2 \text{ N}) \hat{i} + (136 \text{ N}) \hat{j}$$



Vector Review: Components Calculate the *x* **and** *y* **components of the following force vectors!**

$$\vec{F}_2 = 23.5 \text{ N [SW]}$$

What angle is southwest?

$$\theta = 180^{\circ} + 45^{\circ} = 225^{\circ}$$

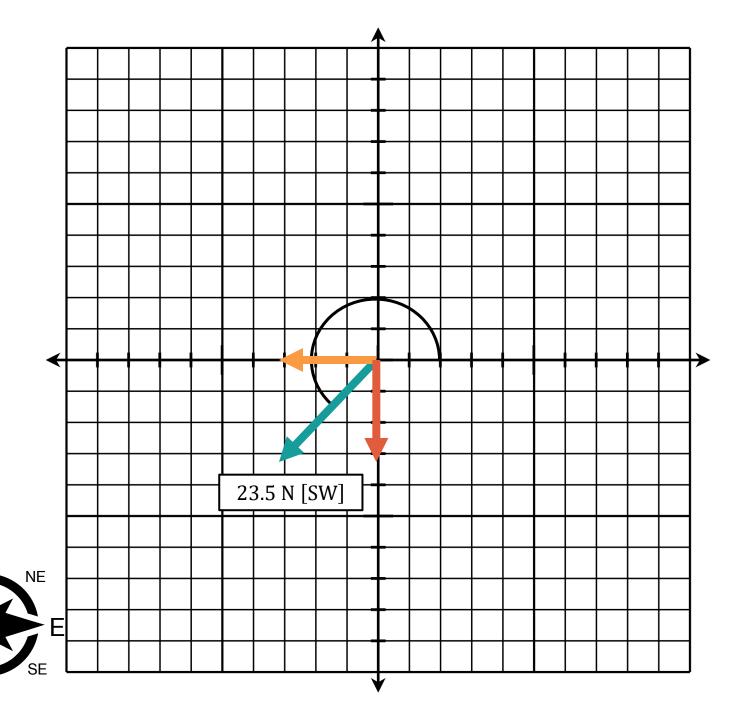
$$F_{x} = (23.5 \text{ N}) \cos 225^{\circ}$$

= -16.6 N

$$F_y = (166 \text{ N}) \sin 125^\circ$$

= -16.6 N

$$\vec{F}_2 = (-16.6 \text{ N})\hat{i} - (16.6 \text{ N})\hat{j}$$



$-\sqrt{3} \hat{j}$ 2 [300°]

Summary: Vector Representation

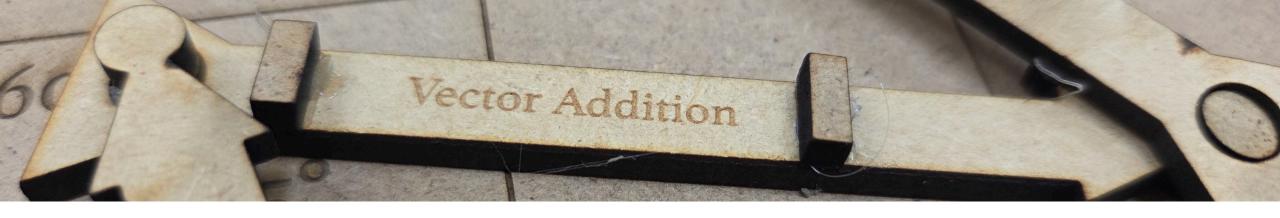
All of the following are representations of the same vector:

- *1.* 2 [300°]
- 2. 2 [S30°E]
- 3. $2 [30^{\circ} E \text{ of S}]$
- 4. $\hat{\imath} \sqrt{3} \, \hat{\jmath}$
- 5. $(1, -\sqrt{3})$
- 6. $(1, -\sqrt{3})$

Any of these formats are acceptable, but **4 and 1** are the best!

Adding Vectors

Activity



Each of these arrows represents a unit vector.

Starting from the **origin** in the centre of the board, multiple vectors can be combined together to make a **resultant vector**.

Experiment with different ways to find the **magnitude** and **angle** of the resultant vectors of the following additions (recall that for a unit vector, the magnitude is always equal to 1):

1.
$$\theta_1 = 0^{\circ}$$
, $\theta_2 = 90^{\circ}$

2.
$$\theta_3 = 30^{\circ}$$
, $\theta_4 = 270^{\circ}$

3.
$$\theta_5 = 135^{\circ}$$
, $\theta_6 = 30^{\circ}$

4.
$$\theta_7 = 180^{\circ}$$
, $\theta_8 = 240^{\circ}$

5.
$$\theta_9 = 0^{\circ}$$
, $\theta_{10} = 0^{\circ}$

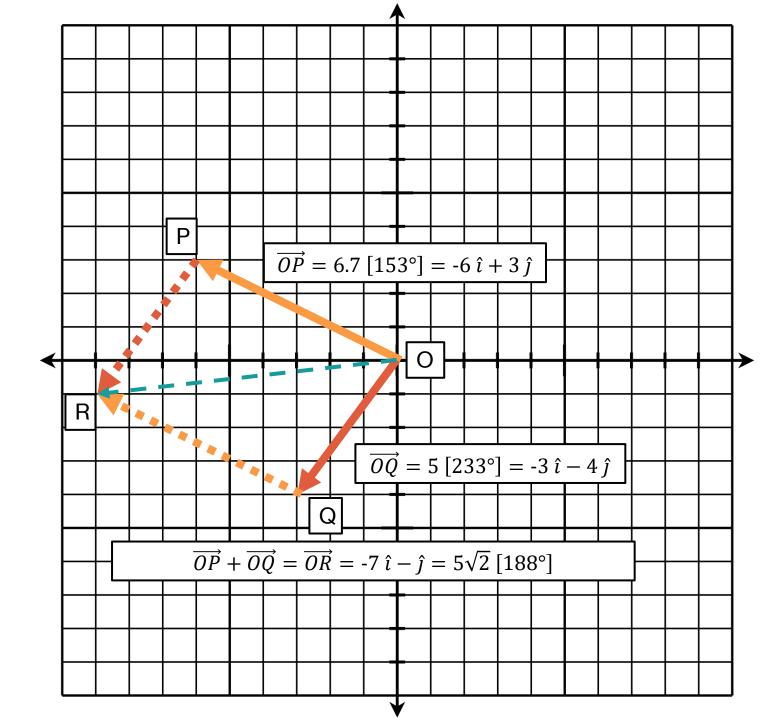
How might you **subtract** a vector instead of adding?

Activity

Vector Addition: Methods

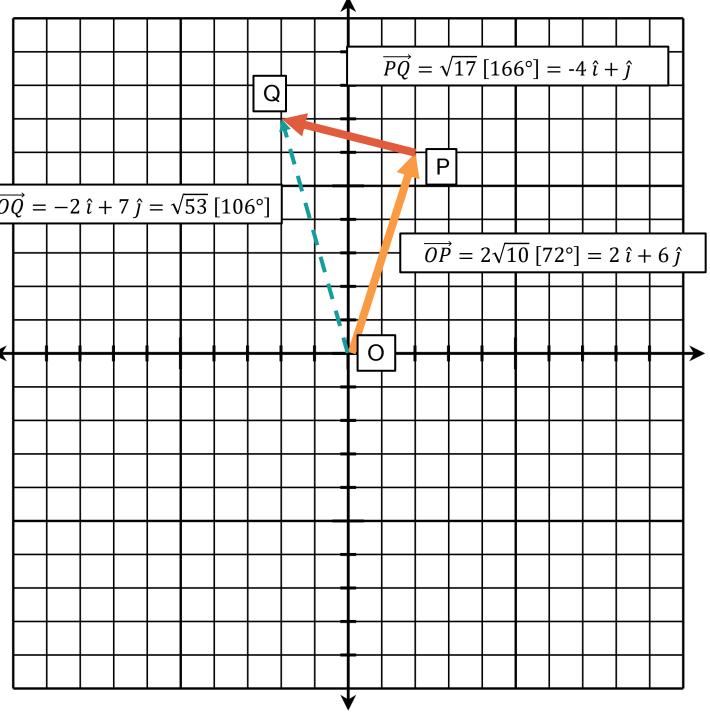
Method 1: Parallelogram

- Put the vectors together, tail to tail.
- 2. Create a **parallelogram** using these two vectors.
- 3. Find the **diagonal** of the parallelogram. This is the **resultant vector** of the vector sum.



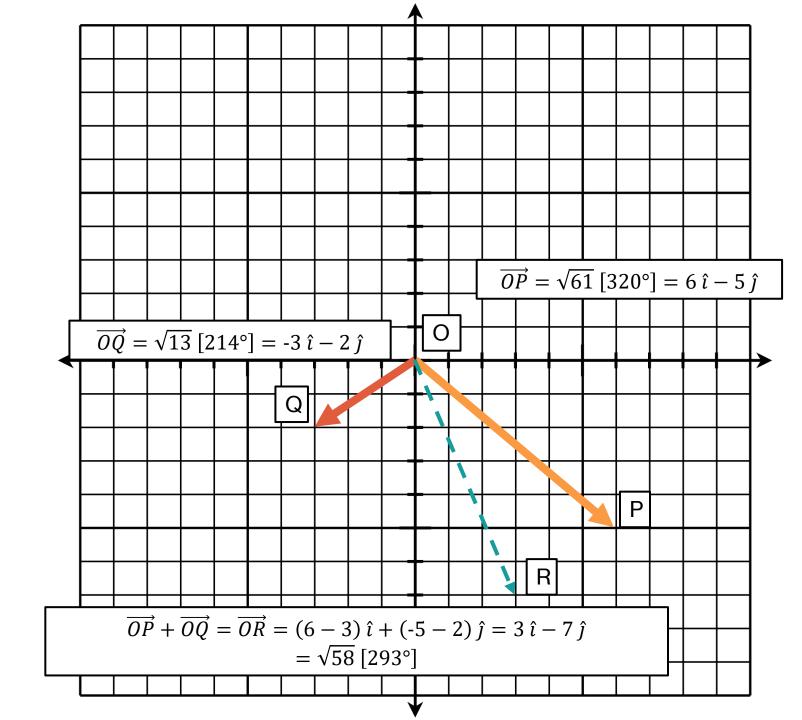
Method 2: **Triangle**

- $\overrightarrow{OP} + \overrightarrow{PQ} = \overrightarrow{OQ} = -2 \hat{\imath} + 7 \hat{\jmath} = \sqrt{53} [106^{\circ}]$
- Put the vectors together, **tail to** head.
- 2. Create a **triangle** using these two vectors.
- 3. Find the **third side** of the triangle. This is the **resultant vector** of the vector sum.



Method 3: Components

- 1. Find the **components** of each vector.
- 2. Add the x and y components.
- 3. The sums of each component are the components of the resultant vector.



Vector Subtraction

How might **subtraction** of vectors work?

- 1. Find the **opposite vector** of the subtracted vector!
- 2. Find the sum of the **positive** vector and the **opposite** vector!

